

Fig. 14. A clamped-free eccentric stiffened shell.



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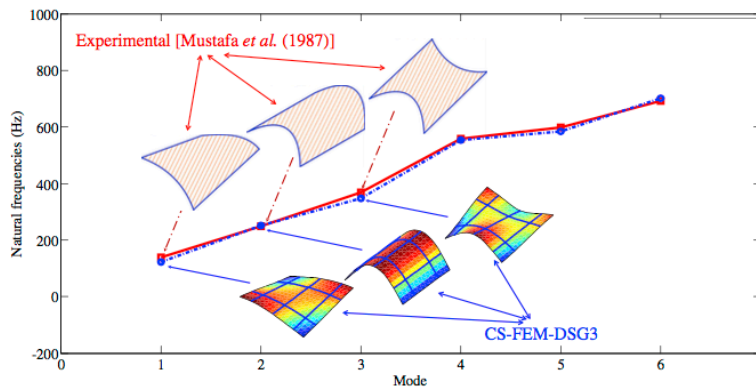


Fig. 15. Six first natural frequencies (Hz) of the orthogonally stiffened free-free cylindrical shell panel.

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See:

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### **Selected Publications:**

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