

Table 1 Glossary of variables used in the generic case, “tank2” (skirt-supported propellant tank) (This is part of the tank2.DEF file, created automatically by the GENOPT processor, GENTEXT, with use of information, variable names and one-line definitions provided by the GENOPT user.)

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C  ARRAY  NUMBER OF          PROMPT
C  ?      (ROWS, COLS)  ROLE  NUMBER  NAME          DEFINITION OF VARIABLE
C                                     (tank2.PRO)
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C  n      ( 0,  0)      2      10  GRAV          = acceleration of gravity
C  n      ( 0,  0)      2      20  DIAVEH        = diameter of launch vehicle
C  n      ( 0,  0)      2      30  AFTDIA        = diameter of the aft dome of the tank
C  n      ( 0,  0)      2      35  AFTHI         = height of the aft dome of the tank
C  n      ( 0,  0)      2      40  FWDDIA        = diameter of the forward dome of the tank
C  n      ( 0,  0)      2      45  FWDHI         = height of the forward dome of the tank
C  n      ( 0,  0)      2      50  FLTANK        = axial dist. from aft dome apex to fwd dome apex
C  n      ( 0,  0)      2      55  ZAPEX         = global axial coordinate of the aft dome apex
C  n      ( 0,  0)      2      60  DENPRP        = weight density of the propellant
C  n      ( 0,  0)      2      65  ZCG           = global axial coordinate of the tank cg
C  n      ( 0,  0)      1      70  THKAFT        = thickness of the tank aft dome skin
C  n      ( 0,  0)      1      75  THKMID        = thickness of the tank cylinder skin
C  n      ( 0,  0)      1      80  THKFWD        = thickness of the forward tank dome skin
C  n      ( 0,  0)      1      90  STRSPC        = spacing of the tank orthogrid stringers
C  n      ( 0,  0)      1      95  RNGSPC        = spacing of the tank orthogrid rings
C  n      ( 0,  0)      1     100  STRTHK        = thickness of the tank orthogrid stringers
C  n      ( 0,  0)      1     105  STRHI         = height of the tank orthogrid stringers
C  n      ( 0,  0)      1     110  RNGTHK        = thickness of the tank orthogrid rings
C  n      ( 0,  0)      1     115  RNGHI         = height of the tank orthogrid rings
C  n      ( 0,  0)      2     125  ETANK         = Young's modulus of the cold tank material
C  n      ( 0,  0)      2     130  NUTANK        = Poisson's ratio of the tank material
C  n      ( 0,  0)      2     135  DENTNK        = mass density of the tank material
C  n      ( 0,  0)      2     140  ALTNK         = coef.thermal expansion of tank material
C  n      ( 0,  0)      2     150  IAXIS         = tank is vertical (1) or horizontal (2)
C  n      ( 0,  0)      2     160  IZTANK        = skirt support ring number in ZTANK(IZTANK)
C  y      ( 2,  0)      1     165  ZTANK         = global axial coordinate of tank support ring
C  y      ( 2,  0)      1     170  ZGRND         = global axial coordinate of "ground"
C  y      ( 2,  0)      2     180  RNGTYP        = propellant tank reinforcement type
C  n      ( 0,  0)      2     190  IDUBAXL       = propellant tank reinforcement type number in
DUBAXL( IDUBAXL)
C  y      ( 2,  0)      1     195  DUBAXL        = axial length of the propellant tank doubler
C  y      ( 2,  0)      1     200  DUBTHK        = max.thickness of the propellant tank doubler
C  y      ( 2,  0)      1     210  TRNGTH        = thickness of the tank reinforcement ring
C  y      ( 2,  0)      1     215  TRNGHI        = height of the tank reinforcement ring
C  y      ( 2,  0)      2     220  TRNGE         = hoop modulus of the tank ring
C  y      ( 2,  0)      2     225  ALRNGT        = coef.of thermal expansion of the tank ring
C  n      ( 0,  0)      2     235  ISKRTYP       = skirt type number in SKRTYP(ISKRTYP)
C  y      ( 2,  0)      2     240  SKRTYP        = skirt type index
C  y      ( 2,  0)      1     250  LNGTNK1       = tank-end length of one-layered skirt part
C  y      ( 2,  0)      1     255  THKTNK1       = tank-end thickness of tapered skirt part
C  y      ( 2,  0)      1     260  LNGTNK2       = tank-end length of tapered prongs
C  y      ( 2,  0)      1     265  THKTNK2       = tank-end thickness of one tapered prong
C  y      ( 2,  0)      1     270  LNGVEH1       = "ground" end length of one-layered skirt part
C  y      ( 2,  0)      1     275  THKVEH1       = "ground"-end thickness of tapered skirt part
C  y      ( 2,  0)      1     280  LNGVEH2       = "ground"-end length of tapered prongs
C  y      ( 2,  0)      1     285  THKVEH2       = "ground"-end thickness of one tapered prong
C  y      ( 2,  0)      2     300  WALTYP        = type of wall constructions in skirt type SKRTYP
C  n      ( 0,  0)      2     310  ITHICK        = thickness index in THICK(ITHICK)
C  y      ( 15,  0)     1     315  THICK         = thickness of a lamina

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C	y	(15, 0)	1	320	ANGLE	= layup angle
C	y	(15, 0)	2	325	MATTYP	= Material type
C	n	(0, 0)	2	335	JLAYTYP	= wall type number in LAYTYP(ILAYTYP,JLAYTYP)
C	n	(0, 0)	2	340	ILAYTYP	= layer number in LAYTYP(ILAYTYP,JLAYTYP)
C	y	(90, 2)	2	345	LAYTYP	= layer type index
C	n	(0, 0)	2	355	IE1	= material type in E1(IE1)
C	y	(2, 0)	2	360	E1	= modulus in the fiber direction
C	y	(2, 0)	2	365	E2	= modulus transverse to fibers
C	y	(2, 0)	2	370	G12	= in-plane shear modulus
C	y	(2, 0)	2	375	NU	= small Poisson's ratio
C	y	(2, 0)	2	380	G13	= x-z out-of-plane shear modulus
C	y	(2, 0)	2	385	G23	= y-z out-of-plane shear modulus
C	y	(2, 0)	2	390	ALPHA1	= coef.of thermal expansion along fibers
C	y	(2, 0)	2	395	ALPHA2	= coef.of thermal expan.transverse to fibers
C	y	(2, 0)	2	400	TEMTUR	= curing delta temperature (positive)
C	y	(2, 0)	2	405	COND1	= conductivity along the fibers
C	y	(2, 0)	2	410	COND2	= conductivity transverse to fibers
C	y	(2, 0)	2	415	DENSTY	= weight density of the material
C	n	(0, 0)	2	425	WGT	= objective=WGT*(empty tank mass) +(1-
WGT)*(conductance)						
C	n	(0, 0)	2	430	TNKNRM	= normalizing empty tank mass
C	n	(0, 0)	2	435	CONNRM	= normalizing total skirt conductance
C	n	(0, 0)	2	445	IPHASE	= IPHASE=1=launch phase; IPHASE=2=orbital phase
C	n	(0, 0)	2	455	NCASES	= Number of load cases (number of environments) in
PRESS(NCASES)						
C	y	(20, 0)	3	460	PRESS	= propellant tank ullage pressure
C	y	(20, 0)	3	465	GAXIAL	= quasi-static axial g-loading
C	y	(20, 0)	3	470	GLATRL	= quasi-static lateral g-loading
C	y	(20, 0)	3	475	TNKCOOL	= propellant tank cool-down from cryogen
C	n	(0, 0)	2	485	JFREQ	= vibration mode type in FREQ(NCASES,JFREQ)
C	y	(20, 4)	4	490	FREQ	= free vibration frequency (cps)
C	y	(20, 4)	5	495	FREQA	= minimum allowable frequency (cps)
C	y	(20, 4)	6	500	FREQF	= factor of safety for frequency
C	n	(0, 0)	2	510	JSTRES1	= stress component number in STRES1(NCASES,JSTRES1)
C	y	(20, 6)	4	515	STRES1	= maximum stress in material 1
C	y	(20, 6)	5	520	STRES1A	= maximum allowable stress in material 1
C	y	(20, 6)	6	525	STRES1F	= factor of safety for stress, matl 1
C	y	(20, 6)	4	530	STRES2	= maximum stress in material 2
C	y	(20, 6)	5	535	STRES2A	= maximum allowable stress in material 2
C	y	(20, 6)	6	540	STRES2F	= factor of safety for stress, matl 2
C	n	(0, 0)	2	550	JSHLBUK	= skirt number (1 for aft skirt) in
SHLBUK(NCASES,JSHLBUK)						
C	y	(20, 2)	4	555	SHLBUK	= buckling of skirt as a shell
C	y	(20, 2)	5	560	SHLBUKA	= allowable for shell buckling of skirt
C	y	(20, 2)	6	565	SHLBUKF	= factor of safety for shell buckling of skirt
C	y	(20, 2)	4	570	FORCE	= launch-hold force in a skirt
C	y	(20, 2)	5	575	FORCEA	= maximum allowable launch-hold force in skirt
C	y	(20, 2)	6	580	FORCEF	= factor of safety for launch-hold force
C	y	(20, 2)	4	585	TNKSTR	= maximum stress in the propellant tank
C	y	(20, 2)	5	590	TNKSTRA	= allowable for propellant tank stress
C	y	(20, 2)	6	595	TNKSTRF	= factor of safety for tank stress
C	y	(20, 2)	4	600	TNKBUK	= propellant tank buckling load factor
C	y	(20, 2)	5	605	TNKBUKA	= allowable for propellant tank buckling
C	y	(20, 2)	6	610	TNKBUKF	= factor of safety for tank buckling
C	n	(0, 0)	7	620	CONDCT	= WGTxTOTMAS/TNKNRM +(1-WGT)xCONDCT/CONNRM

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**Table 2 Input data for the GENOPT processor, BEGIN (oneskirt.BEG file)
(These input data are provided by the End user for the generic case called
“tank2” and the specific case called “oneskirt”).**

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      N          $ Do you want a tutorial session and tutorial output?
386.4000      $ acceleration of gravity: GRAV
      300        $ diameter of launch vehicle: DIAVEH
      200        $ diameter of the aft dome of the tank: AFTDIA
      50         $ height of the aft dome of the tank: AFTHI
      200        $ diameter of the forward dome of the tank: FWDDIA
      50         $ height of the forward dome of the tank: FWDHI
      400        $ axial dist. from aft dome apex to fwd dome apex: FLTANK
      100        $ global axial coordinate of the aft dome apex: ZAPEX
0.2560000E-02 $ weight density of the propellant: DENPRP
      300        $ global axial coordinate of the tank cg: ZCG
0.1000000    $ thickness of the tank aft dome skin: THKAFT
0.1000000    $ thickness of the tank cylinder skin: THKMID
0.1000000    $ thickness of the forward tank dome skin: THKFWD
      10         $ spacing of the tank orthogrid stringers: STRSPC
      10         $ spacing of the tank orthogrid rings: RNGSPC
0.5000000    $ thickness of the tank orthogrid stringers: STRTHK
      1          $ height of the tank orthogrid stringers: STRHI
0.5000000    $ thickness of the tank orthogrid rings: RNGTHK
      1          $ height of the tank orthogrid rings: RNGHI
0.1000000E+08 $ Young's modulus of the cold tank material: ETANK
0.3000000    $ Poisson's ratio of the tank material: NUTANK
0.2500000E-03 $ mass density of the tank material: DENTNK
0.1000000E-04 $ coef.thermal expansion of tank material: ALTNK
      1          $ tank is vertical (1) or horizontal (2): IAXIS
      1          $ Number IZTANK of rows in the array ZTANK: IZTANK
      300        $ global axial coordinate of tank support ring: ZTANK( 1)
      50         $ global axial coordinate of "ground": ZGRND( 1)
      1          $ propellant tank reinforcement type: RNGTYP( 1)
      1          $ Number IDUBAXL of rows in the array DUBAXL: IDUBAXL
      30         $ axial length of the propellant tank doubler: DUBAXL( 1)
0.1000000    $ max.thickness of the propellant tank doubler: DUBTHK( 1)
0.2000000    $ thickness of the tank reinforcement ring: TRNGTH( 1)
      1.000000    $ height of the tank reinforcement ring: TRNGHI( 1)
0.1000000E+08 $ hoop modulus of the tank ring: TRNGE( 1)
0.1000000E-04 $ coef.of thermal expansion of the tank ring: ALRNGT( 1)
      1          $ Number ISKRTYP of rows in the array SKRTYP: ISKRTYP
      1          $ skirt type index: SKRTYP( 1)
      5          $ tank-end length of one-layered skirt part: LNGTNK1( 1)
0.2500000    $ tank-end thickness of tapered skirt part: THKTNK1( 1)
      5          $ tank-end length of tapered prongs: LNGTNK2( 1)
0.5000000E-01 $ tank-end thickness of one tapered prong: THKTNK2( 1)
      5          $ "ground" end length of one-layered skirt part: LNGVEH1( 1)
0.2500000    $ "ground"-end thickness of tapered skirt part: THKVEH1( 1)
      5          $ "ground"-end length of tapered prongs: LNGVEH2( 1)

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0.5000000E-01 $ "ground"-end thickness of one tapered prong: TNKVEH2( 1)
      1      $ type of wall constructions in skirt type SKRTYP: WALTYP( 1)
      6      $ Number ITHICK of rows in the array THICK: ITHICK
0.3000000E-01 $ thickness of a lamina: THICK( 1)
0.3000000E-01 $ thickness of a lamina: THICK( 2)
0.3000000E-01 $ thickness of a lamina: THICK( 3)
0.3000000E-01 $ thickness of a lamina: THICK( 4)
0.3000000E-01 $ thickness of a lamina: THICK( 5)
0.3000000E-01 $ thickness of a lamina: THICK( 6)
      45     $ layup angle: ANGLE( 1)
     -45     $ layup angle: ANGLE( 2)
      45     $ layup angle: ANGLE( 3)
     -45     $ layup angle: ANGLE( 4)
      45     $ layup angle: ANGLE( 5)
     -45     $ layup angle: ANGLE( 6)
      1      $ Material type: MATTYP( 1)
      1      $ Material type: MATTYP( 2)
      1      $ Material type: MATTYP( 3)
      1      $ Material type: MATTYP( 4)
      1      $ Material type: MATTYP( 5)
      1      $ Material type: MATTYP( 6)
      1      $ Number JLAYTYP of columns in the array, LAYTYP: JLAYTYP
     12     $ Number ILAYTYP of rows in this column of LAYTYP: ILAYTYP
      1      $ layer type index: LAYTYP( 1, 1)
      2      $ layer type index: LAYTYP( 2, 1)
      3      $ layer type index: LAYTYP( 3, 1)
      4      $ layer type index: LAYTYP( 4, 1)
      5      $ layer type index: LAYTYP( 5, 1)
      6      $ layer type index: LAYTYP( 6, 1)
      6      $ layer type index: LAYTYP( 7, 1)
      5      $ layer type index: LAYTYP( 8, 1)
      4      $ layer type index: LAYTYP( 9, 1)
      3      $ layer type index: LAYTYP( 10, 1)
      2      $ layer type index: LAYTYP( 11, 1)
      1      $ layer type index: LAYTYP( 12, 1)
      1      $ Number IE1 of rows in the array E1: IE1
0.2100000E+08 $ modulus in the fiber direction: E1( 1)
     160000. $ modulus transverse to fibers: E2( 1)
     679000.0 $ in-plane shear modulus: G12( 1)
0.2300000E-01 $ small Poisson's ratio: NU( 1)
     627000.0 $ x-z out-of-plane shear modulus: G13( 1)
     334000.0 $ y-z out-of-plane shear modulus: G23( 1)
0.1000000E-05 $ coef.of thermal expansion along fibers: ALPHA1( 1)
0.1000000E-04 $ coef.of thermal expan.transverse to fibers: ALPHA2( 1)
      000     $ curing delta temperature (positive): TEMTUR( 1)
0.7270000E-02 $ conductivity along the fibers: COND1( 1)
0.4370000E-02 $ conductivity transverse to fibers: COND2( 1)
0.5700000E-01 $ weight density of the material: DENSTY( 1)
0.5000000     $ objective=WGT*(empty tank mass) +(1-WGT)*(conductance): WGT
     10.00000 $ normalizing empty tank mass: TNKNRM
0.2000000E-02 $ normalizing total skirt conductance: CONNRM
      1      $ IPHASE=1=launch phase; IPHASE=2=orbital phase: IPHASE
      2      $ Number NCASES of load cases (environments): NCASES
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25      $ propellant tank ullage pressure: PRESS( 1)
25      $ propellant tank ullage pressure: PRESS( 2)
10      $ quasi-static axial g-loading: GAXIAL( 1)
0       $ quasi-static axial g-loading: GAXIAL( 2)
0       $ quasi-static lateral g-loading: GLATRL( 1)
-10     $ quasi-static lateral g-loading: GLATRL( 2)
-200    $ propellant tank cool-down from cryogen: TNKCOOL( 1)
-200    $ propellant tank cool-down from cryogen: TNKCOOL( 2)
4       $ Number JFREQ of columns in the array, FREQ: JFREQ
10      $ minimum allowable frequency (cps): FREQA( 1, 1)
10      $ minimum allowable frequency (cps): FREQA( 2, 1)
10      $ minimum allowable frequency (cps): FREQA( 1, 2)
10      $ minimum allowable frequency (cps): FREQA( 2, 2)
10      $ minimum allowable frequency (cps): FREQA( 1, 3)
10      $ minimum allowable frequency (cps): FREQA( 2, 3)
10      $ minimum allowable frequency (cps): FREQA( 1, 4)
10      $ minimum allowable frequency (cps): FREQA( 2, 4)
1.200000 $ factor of safety for frequency: FREQF( 1, 1)
1.200000 $ factor of safety for frequency: FREQF( 2, 1)
1.200000 $ factor of safety for frequency: FREQF( 1, 2)
1.200000 $ factor of safety for frequency: FREQF( 2, 2)
1.200000 $ factor of safety for frequency: FREQF( 1, 3)
1.200000 $ factor of safety for frequency: FREQF( 2, 3)
1.200000 $ factor of safety for frequency: FREQF( 1, 4)
1.200000 $ factor of safety for frequency: FREQF( 2, 4)
5       $ Number JSTRES1 of columns in the array, STRES1: JSTRES1
140571  $ maximum allowable stress in material 1: STRES1A( 1, 1)
140571  $ maximum allowable stress in material 1: STRES1A( 2, 1)
104714  $ maximum allowable stress in material 1: STRES1A( 1, 2)
104714  $ maximum allowable stress in material 1: STRES1A( 2, 2)
10557   $ maximum allowable stress in material 1: STRES1A( 1, 3)
10557   $ maximum allowable stress in material 1: STRES1A( 2, 3)
14529   $ maximum allowable stress in material 1: STRES1A( 1, 4)
14529   $ maximum allowable stress in material 1: STRES1A( 2, 4)
6290    $ maximum allowable stress in material 1: STRES1A( 1, 5)
6290    $ maximum allowable stress in material 1: STRES1A( 2, 5)
1.500000 $ factor of safety for stress, matl 1: STRES1F( 1, 1)
1.500000 $ factor of safety for stress, matl 1: STRES1F( 2, 1)
1.500000 $ factor of safety for stress, matl 1: STRES1F( 1, 2)
1.500000 $ factor of safety for stress, matl 1: STRES1F( 2, 2)
1.500000 $ factor of safety for stress, matl 1: STRES1F( 1, 3)
1.500000 $ factor of safety for stress, matl 1: STRES1F( 2, 3)
1.500000 $ factor of safety for stress, matl 1: STRES1F( 1, 4)
1.500000 $ factor of safety for stress, matl 1: STRES1F( 2, 4)
1.500000 $ factor of safety for stress, matl 1: STRES1F( 1, 5)
1.500000 $ factor of safety for stress, matl 1: STRES1F( 2, 5)
140571  $ maximum allowable stress in material 2: STRES2A( 1, 1)
140571  $ maximum allowable stress in material 2: STRES2A( 2, 1)
104714  $ maximum allowable stress in material 2: STRES2A( 1, 2)
104714  $ maximum allowable stress in material 2: STRES2A( 2, 2)
10557   $ maximum allowable stress in material 2: STRES2A( 1, 3)
10557   $ maximum allowable stress in material 2: STRES2A( 2, 3)
14529   $ maximum allowable stress in material 2: STRES2A( 1, 4)
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14529    $ maximum allowable stress in material 2: STRES2A( 2, 4)
 6290    $ maximum allowable stress in material 2: STRES2A( 1, 5)
 6290    $ maximum allowable stress in material 2: STRES2A( 2, 5)
1.500000 $ factor of safety for stress, matl 2: STRES2F( 1, 1)
1.500000 $ factor of safety for stress, matl 2: STRES2F( 2, 1)
1.500000 $ factor of safety for stress, matl 2: STRES2F( 1, 2)
1.500000 $ factor of safety for stress, matl 2: STRES2F( 2, 2)
1.500000 $ factor of safety for stress, matl 2: STRES2F( 1, 3)
1.500000 $ factor of safety for stress, matl 2: STRES2F( 2, 3)
1.500000 $ factor of safety for stress, matl 2: STRES2F( 1, 4)
1.500000 $ factor of safety for stress, matl 2: STRES2F( 2, 4)
1.500000 $ factor of safety for stress, matl 2: STRES2F( 1, 5)
1.500000 $ factor of safety for stress, matl 2: STRES2F( 2, 5)
 2      $ Number JSHLBUK of columns in the array, SHLBUK: JSHLBUK
 1      $ allowable for shell buckling of skirt: SHLBUKA( 1, 1)
 1      $ allowable for shell buckling of skirt: SHLBUKA( 2, 1)
 1      $ allowable for shell buckling of skirt: SHLBUKA( 1, 2)
 1      $ allowable for shell buckling of skirt: SHLBUKA( 2, 2)
 2      $ factor of safety for shell buckling of skirt: SHLBUKF( 1, 1)
 2      $ factor of safety for shell buckling of skirt: SHLBUKF( 2, 1)
 2      $ factor of safety for shell buckling of skirt: SHLBUKF( 1, 2)
 2      $ factor of safety for shell buckling of skirt: SHLBUKF( 2, 2)
15000   $ maximum allowable launch-hold force in skirt: FORCEA( 1, 1)
15000   $ maximum allowable launch-hold force in skirt: FORCEA( 2, 1)
15000   $ maximum allowable launch-hold force in skirt: FORCEA( 1, 2)
15000   $ maximum allowable launch-hold force in skirt: FORCEA( 2, 2)
 1      $ factor of safety for launch-hold force: FORCEF( 1, 1)
 1      $ factor of safety for launch-hold force: FORCEF( 2, 1)
 1      $ factor of safety for launch-hold force: FORCEF( 1, 2)
 1      $ factor of safety for launch-hold force: FORCEF( 2, 2)
50000   $ allowable for propellant tank stress: TNKSTRA( 1, 1)
50000   $ allowable for propellant tank stress: TNKSTRA( 2, 1)
50000   $ allowable for propellant tank stress: TNKSTRA( 1, 2)
50000   $ allowable for propellant tank stress: TNKSTRA( 2, 2)
 1.5    $ factor of safety for tank stress: TNKSTRF( 1, 1)
 1.5    $ factor of safety for tank stress: TNKSTRF( 2, 1)
 1.5    $ factor of safety for tank stress: TNKSTRF( 1, 2)
 1.5    $ factor of safety for tank stress: TNKSTRF( 2, 2)
 1      $ allowable for propellant tank buckling: TNKBUKA( 1, 1)
 1      $ allowable for propellant tank buckling: TNKBUKA( 2, 1)
 1      $ allowable for propellant tank buckling: TNKBUKA( 1, 2)
 1      $ allowable for propellant tank buckling: TNKBUKA( 2, 2)
 2.0    $ factor of safety for tank buckling: TNKBUKF( 1, 1)
 2.0    $ factor of safety for tank buckling: TNKBUKF( 2, 1)
 2.0    $ factor of safety for tank buckling: TNKBUKF( 1, 2)
 2.0    $ factor of safety for tank buckling: TNKBUKF( 2, 2)
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FOOTNOTE: Some Conventions are as follows:
An "A" added to a behavioral variable name means "allowable"
An "F" added to a behavioral variable name means "factor of safety"
Array Indices, i,j,k:

FREQ(i,j) = modal vibration frequency: i = load case; j = vibration mode

j = 1 means first eigenvalue for n = 0 waves (usually the mode with significant axial motion of the tank)

j = 2 means first eigenvalue for n = 1 waves (a mode with significant lateral-pitch motion of the tank)

j = 3 means first eigenvalue for n = 2 waves (a mode in which the tank wall deforms with 2 circ. waves)

j = 4 means first eigenvalue for n = 3 or 4 waves (a mode in which the tank wall deforms)

STRESSi(j,k) = stress component in strut: i = material no., j=load case, k = stress component

i = 1 means "material no. 1" which also means "strut type no. 1" (aft ring of struts)

i = 2 means "material no. 2" which also means "strut type no. 2" (forward ring of struts)

j = 1 means "Load Case 1" (See the section above entitled TWO LOAD CASES)

j = 2 means "Load Case 2" (See the section above entitled TWO LOAD CASES)

k = 1 means tension along the fibers of a ply

k = 2 means compression along the fibers of a ply

k = 3 means tension transverse to the fibers of a ply

k = 4 means compression transverse to the fibers of a ply

k = 5 means in-plane shear in a ply

SHLBUK(i,j) = buckling of the strut as a thin shell: i = load case; j = strut type

j = 1 means the type of strut attached to the aft propellant tank support ring.

j = 2 means the type of strut attached to the forward propellant tank support ring.

TNKSTR(i,j) = maximum effective stress: i = load case; j = meridian number

j = 1 = effective stress in the tank is the maximum from the distribution along meridian no. 1

j = 2 = effective stress in the tank is the maximum from the distribution along meridian no. 2

TNKBUK(i,j) = buckling load factor: i = load case; j = meridian number

j = 1 means buckling load factor of the tank from the prebuckling stress distribution along meridian no. 1

j = 2 means buckling load factor of the tank from the prebuckling stress distribution along meridian no. 2

Table 3 Maximum stresses (psi) in the optimized “oneskirt” configuration under Load Cases 1 and 2 predicted by the GENOPT/BIGBOSOR4 model

Load Case 1 (10g axial acceleration, 25 psi ullage pressure, 200 deg. tank cool-down):

Stress= 9.1942E+02 fiber tension : matl=2 , A , seg=3 , node=90 , layer=12 , z= 0.17 ;FS= 1.50
 Stress= 3.3538E+04 fiber tension : matl=3 , A , seg=17 , node=7 , layer=1 , z=-0.49 ;FS= 1.50
 Stress= 1.8489E+04 fiber compres.: matl=2 , A , seg=4 , node=13 , layer=11 , z= 0.12 ;FS= 1.50
 Stress= 5.8708E+03 fiber compres.: matl=3 , A , seg=21 , node=50 , layer=1 , z=-0.43 ;FS= 1.50
 Stress= 2.4409E+03 transv tension: matl=2 , A , seg=3 , node=94 , layer=10 , z= 0.12 ;FS= 1.50
 Stress= 2.9366E+04 transv tension: matl=3 , A , seg=18 , node=7 , layer=1 , z=-0.03 ;FS= 1.50
 Stress= 4.1398E+02 transv compres: matl=2 , A , seg=3 , node=2 , layer=1 , z=-0.17 ;FS= 1.50
 Stress= 1.7041E+04 transv compres: matl=3 , A , seg=23 , node=5 , layer=1 , z=-0.44 ;FS= 1.50
 Stress= 5.6036E+02 in-plane shear: matl=2 , A , seg=3 , node=94 , layer=3 , z=-0.12 ;FS= 1.50
 Stress= 2.1462E+04 effect. stress: matl=1 , A , seg=4 , node=2 , layer=14 , z= 0.18 ;FS= 1.50
 Stress= 1.8987E+04 effect. stress: matl=4 , A , seg=16 , node=9 , layer=2 , z=-0.09 ;FS= 1.50
 Stress= 2.8270E+04 effect. stress: matl=5 , A , seg=19 , node=2 , layer=3 , z= 0.03 ;FS= 1.50
 Stress= 3.1977E+04 effect. stress: matl=6 , A , seg=18 , node=6 , layer=2 , z= 0.03 ;FS= 1.50
 Stress= 2.1141E+04 effect. stress: matl=7 , A , seg=33 , node=13 , layer=2 , z= 0.04 ;FS= 1.50

Modified maximum stress components for Load Case 1 STRESS2(i),i=1,6=

fiber tension	fiber compres.	transv tension	transv compres	in-plane shear	effect. stress
3.3538E+04	8.8282E+03	2.9366E+04	1.7041E+04	4.4544E+03	3.1977E+04

Load Case 2 (10g lateral acceleration, 25 psi ullage pressure, 200 deg. tank cool-down):

Stress= 1.8841E+03 fiber tension : matl=2 , A , seg=3 , node=9 , layer=12 , z= 0.17 ;FS= 1.50
 Stress= 3.3333E+04 fiber tension : matl=3 , A , seg=22 , node=8 , layer=1 , z=-0.44 ;FS= 1.50
 Stress= 1.6076E+04 fiber compres.: matl=2 , A , seg=4 , node=13 , layer=11 , z= 0.12 ;FS= 1.50
 Stress= 6.8810E+03 fiber compres.: matl=3 , A , seg=21 , node=50 , layer=1 , z=-0.43 ;FS= 1.50
 Stress= 2.4820E+03 transv tension: matl=2 , A , seg=3 , node=93 , layer=10 , z= 0.12 ;FS= 1.50
 Stress= 2.6867E+04 transv tension: matl=3 , A , seg=21 , node=47 , layer=1 , z=-0.03 ;FS= 1.50
 Stress= 1.4473E+03 transv compres: matl=2 , A , seg=3 , node=2 , layer=1 , z=-0.17 ;FS= 1.50
 Stress= 1.8667E+04 transv compres: matl=3 , A , seg=23 , node=5 , layer=1 , z=-0.44 ;FS= 1.50
 Stress= 6.0517E+02 in-plane shear: matl=2 , A , seg=3 , node=5 , layer=3 , z=-0.12 ;FS= 1.50
 Stress= 2.2347E+04 effect. stress: matl=1 , A , seg=4 , node=2 , layer=1 , z=-0.18 ;FS= 1.50
 Stress= 1.4335E+04 effect. stress: matl=4 , A , seg=16 , node=9 , layer=2 , z=-0.09 ;FS= 1.50
 Stress= 2.6055E+04 effect. stress: matl=5 , A , seg=20 , node=12 , layer=3 , z= 0.03 ;FS= 1.50
 Stress= 2.8461E+04 effect. stress: matl=6 , A , seg=21 , node=48 , layer=2 , z= 0.03 ;FS= 1.50
 Stress= 2.3645E+04 effect. stress: matl=7 , A , seg=33 , node=6 , layer=2 , z= 0.04 ;FS= 1.50

Modified maximum stress components for Load Case 2 STRESS2(i),i=1,6=

fiber tension	fiber compres.	transv tension	transv compres	in-plane shear	effect. stress
3.3333E+04	7.6760E+03	2.6867E+04	1.8667E+04	4.8106E+03	2.8461E+04

Table 4 Maximum stresses (psi) in the optimized “twoskirt” configuration under Load Cases 1 and 2 as predicted by GENOPT/BIGBOSOR4

Load Case 1 (10g axial acceleration, 25 psi ullage pressure, 200 deg. tank cool-down):

Stress= 2.7506E+04 fiber tension : matl=2 , A , seg=36, node=7 , layer=10,z= 0.04 ;FS= 1.50
 Stress= 3.3583E+04 fiber tension : matl=3 , A , seg=16, node=5 , layer=1 , z=-0.46 ;FS= 1.50
 Stress= 2.8580E+04 fiber compres.: matl=2, A , seg=4 , node=13, layer=13,z= 0.05 ;FS= 1.50
 Stress= 2.4008E+04 fiber compres.: matl=3, A , seg=22, node=2 , layer=1 , z=-0.44 ;FS= 1.50
 Stress= 4.7809E+03 transv tension: matl=2 , A , seg=36, node=8 , layer=12,z= 0.06 ;FS= 1.50
 Stress= 1.9012E+04 transv tension: matl=3 , A , seg=19, node=3 , layer=1 , z=-0.06 ;FS= 1.50
 Stress= 1.7932E+04 transv compres: matl=3, A , seg=15, node=11, layer=1, z=-0.46 ;FS= 1.50
 Stress= 5.5800E+02 in-plane shear: matl=2 , A , seg=35, node=2 , layer=2 , z=-0.06 ;FS= 1.50
 Stress= 3.2173E+04 effect. stress: matl=1 , A , seg=35, node=2 , layer=1 , z=-0.07 ;FS= 1.50
 Stress= 2.4268E+04 effect. stress: matl=4 , A , seg=6 , node=2 , layer=2 , z = 0.06 ;FS= 1.50
 Stress= 2.4061E+04 effect. stress: matl=5 , A , seg=18, node=12, layer=3, z= 0.07 ;FS= 1.50
 Stress= 2.7316E+04 effect. stress: matl=6 , A , seg=19, node=2 , layer=2 , z= 0.06 ;FS= 1.50
 Stress= 2.3496E+04 effect. stress: matl=7 , A , seg=33, node=13, layer=2, z= 0.04 ;FS= 1.50

Modified maximum stress components for Load Case 1 STRESS2(i),i=1,6=

fiber tension	fiber compres.	transv tension	transv compres	in-plane shear	effect. stress
3.3583E+04	2.4008E+04	2.2643E+04	1.7932E+04	4.4356E+03	3.2173E+04

Load Case 2 (10g lateral acceleration, 25 psi ullage pressure, 200 deg. tank cool-down):

Stress= 3.4188E+04 fiber tension : matl=2 , A , seg=3 , node=93, layer=9 , z= 0.03 ;FS= 1.50
 Stress= 3.4335E+04 fiber tension : matl=3 , A , seg=23, node=9 , layer=1 , z=-0.44 ;FS= 1.50
 Stress= 3.0823E+04 fiber compres.: matl=2 , A , seg=35, node=1 , layer=12, z= 0.05 ;FS= 1.50
 Stress= 2.0893E+04 fiber compres.: matl=3 , A , seg=22, node=2 , layer=1 , z=-0.44 ;FS= 1.50
 Stress= 5.2071E+03 transv tension: matl=2 , A , seg=3 , node=92, layer=12, z= 0.05 ;FS= 1.50
 Stress= 1.8089E+04 transv tension: matl=3 , A , seg=33, node=13, layer=1 , z=-0.04 ;FS= 1.50
 Stress= 8.0684E+01 transv compres: matl=2 , A , seg=36, node=98, layer=10,z= 0.04 ;FS= 1.50
 Stress= 1.7819E+04 transv compres: matl=3 , A , seg=24, node=4 , layer=1 , z=-0.44 ;FS= 1.50
 Stress= 2.1950E+03 in-plane shear: matl=2 , A , seg=4 , node=1 , layer=3 , z=-0.04 ;FS= 1.50
 Stress= 3.4632E+04 effect. stress: matl=1 , A , seg=4 , node=2 , layer=1 , z=-0.05 ;FS= 1.50
 Stress= 1.8883E+04 effect. stress: matl=4 , A , seg=6 , node=2 , layer=2 , z= 0.06 ;FS= 1.50
 Stress= 2.2342E+04 effect. stress: matl=5 , A , seg=18, node=12, layer=3 , z= 0.07 ;FS= 1.50
 Stress= 2.5577E+04 effect. stress: matl=6 , A , seg=19, node=2 , layer=2 , z= 0.06 ;FS= 1.50
 Stress= 2.6047E+04 effect. stress: matl=7 , A , seg=33, node=13, layer=2, z= 0.04 ;FS= 1.50

Modified maximum stress components for Load Case 2 STRESS2(i),i=1,6=

fiber tension	fiber compres.	transv tension	transv compres	in-plane shear	effect. stress
3.4335E+04	2.0893E+04	2.4662E+04	1.7819E+04	1.7448E+04	3.4632E+04

Table 5 Predictions by GENOPT/tank2 of buckling of the aft conical skirt under Load Case 1 for the optimized “twoskirt” configuration

Buckling in the propellant tank/skirt system from the **prebuckling load distribution on the meridian at angle, CIRCANG(JCOL)= 0.0000E+00** in which JCOL = 1
The valid BIGBOSOR4 input file is called: twoskirt.BEHX911

BUCKLING OF THE PROPELLANT TANK/SKIRT SYSTEM FROM THE BIGBOSOR4 MODEL

6.3407E+00	(n= 3 circ.waves);	IFAILD= 0	
6.3295E+00	(n= 5 circ.waves);	IFAILD= 0	
6.3129E+00	(n= 7 circ.waves);	IFAILD= 0	
6.2907E+00	(n= 9 circ.waves);	IFAILD= 0	
6.2631E+00	(n= 11 circ.waves);	IFAILD= 0	
6.2294E+00	(n= 13 circ.waves);	IFAILD= 0	
6.1897E+00	(n= 15 circ.waves);	IFAILD= 0	
6.1437E+00	(n= 17 circ.waves);	IFAILD= 0	
6.0902E+00	(n= 19 circ.waves);	IFAILD= 0	
6.0329E+00	(n= 21 circ.waves);	IFAILD= 0	
5.9862E+00	(n= 23 circ.waves);	IFAILD= 0	
5.9573E+00	(n= 25 circ.waves);	IFAILD= 0	
5.9460E+00	(n= 27 circ.waves);	IFAILD= 0	←critical buckling load factor
5.9520E+00	(n= 29 circ.waves);	IFAILD= 0	
5.9575E+00	(n= 31 circ.waves);	IFAILD= 0	
5.9633E+00	(n= 33 circ.waves);	IFAILD= 0	
5.9873E+00	(n= 35 circ.waves);	IFAILD= 0	
6.0297E+00	(n= 37 circ.waves);	IFAILD= 0	
6.0905E+00	(n= 39 circ.waves);	IFAILD= 0	
6.1694E+00	(n= 41 circ.waves);	IFAILD= 0	
6.2660E+00	(n= 43 circ.waves);	IFAILD= 0	
6.3798E+00	(n= 45 circ.waves);	IFAILD= 0	
6.5102E+00	(n= 47 circ.waves);	IFAILD= 0	
6.6189E+00	(n= 49 circ.waves);	IFAILD= 0	

etc.

PANDA2-type buckling predictions corresponding to the prebuckled state along the skirt meridian at theta= 0.0000E+00 degrees...

In this buckling analysis there are two PANDA2 models:

Model 1: The full length of the effective cylindrical shell is included and N_x, N_y, N_{xy} at the midlength of the skirt are considered to be the prebuckled state which is uniform over the entire PANDA2 model.

Model 2: 1/4th of the length nearest the large-diameter end of the conical skirt is included, and $N_x, 0., N_{xy}$

ten nodal points from the large-diameter end are considered to be the uniform prebuckled state.

We use the minimum of the two buckling load factors from PANDA2 Model 1 and PANDA2 Model 2 as the buckling load obtained from a PANDA2 analysis.

Listed next are the assumed prebuckled state, length and radius of the effective cylindrical shell, buckling mode, (MSKIN,NSKIN,SLOPE), and **buckling load factor for Model 1:** Buckling load factor predicted from a PANDA2-type model of the **aft skirt for Load Case 1:**

Average Load Set A prebuckling resultants used in the PANDA2 model:

Average axial resultant over meridian length, NXAVE = -2.8593E+02

Average hoop resultant over meridian length, NYAVE = -2.9823E+00

Average in-plane shear resultant, NXYAVE= 0.0000E+00

Average Load Set B prebuckling resultants used in the PANDA2 model:

Average axial resultant over meridian length, NXFIX = 1.4326E+03

Average hoop resultant over meridian length, NYFIX = 6.2338E-01

Length of the equivalent cylindrical shell, FLEFF = 1.3928E+02

Radius of the equivalent cylindrical shell, RAVE = 1.3393E+02

Critical buckling mode:

Number of axial half-waves over shell length, MSKIN = 1

Number of circ. half-waves over 180 degrees, NSKIN = 15

Slope of the buckling nodal lines, SLOPE = 0.0000E+00

SLOPE=dy/dx in Fig. 9(b) of 1987 "Theoretical Basis paper.

"Bump-up" factor to adjust for milder imperfection

sensitivity factor when in-plane shear is significant 1.0000E+00

The actual buckling load factor, EIGLOC*FKNOCK/RATIO= 5.6307E+00

PANDA2-type buckling predictions corresponding to the prebuckled state along the skirt meridian at theta= 0.0000E+00 degrees...

Model 2: 1/4th of the length nearest the large-diameter end

of the conical skirt is included, and Nx,0.,Nxy ten nodal points from the large-diameter end are considered to be the uniform prebuckled state.

We use the minimum of the two buckling load factors from PANDA2 Model 1 and PANDA2 Model 2 as the buckling load obtained from a PANDA2 analysis.

Listed next are the assumed prebuckled state, length and radius of the effective cylindrical shell, buckling mode, (MSKIN,NSKIN,SLOPE), and **buckling load factor for Model 2:** Buckling load factor predicted from a PANDA2-type model of the aft skirt for Load Case 1:

Average Load Set A prebuckling resultants used in the PANDA2 model:

Average axial resultant over meridian length, NXAVE = -2.4787E+02

Average hoop resultant over meridian length, NYAVE = 0.0000E+00

Average in-plane shear resultant, NXYAVE= 0.0000E+00

Average Load Set B prebuckling resultants used in the PANDA2 model:

Average axial resultant over meridian length, NXFIX = 1.2235E+03
Average hoop resultant over meridian length, NYFIX = 0.0000E+00
Length of the equivalent cylindrical shell, FLEFF = 3.4821E+01
Radius of the equivalent cylindrical shell, RAVE = 1.6071E+02

Critical buckling mode:

Number of axial half-waves over shell length, MSKIN = 3
Number of circ. half-waves over 180 degrees, NSKIN = 32
Slope of the buckling nodal lines, SLOPE = 1.0167E-01
SLOPE=dy/dx in Fig. 9(b) of 1987 "Theoretical Basis paper."
"Bump-up" factor to adjust for milder imperfection
sensitivity factor when in-plane shear is significant 1.0000E+00
The actual buckling load factor, EIGLOC*FKNOCK/RATIO= 5.6305E+00

Minimum buckling load from PANDA2 Models 1 & 2, EIGMIN= 5.6305E+00
For the buckling load factor, GENOPT/SKIRT uses the minimum
buckling load from PANDA2 for the aft and forward (if any)
skirt(s) and the buckling load from the BIGBOSOR4 model.
The buckling load from the BIGBOSOR4 model is EIGCRT= 5.9460E+00

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Table 6 Predictions by GENOPT/tank2 of buckling of the aft conical skirt under Load Case 2 for the optimized “twoskirt” configuration according to the PANDA-type Model 1 with use of the prebuckling resultants at the midlength of the meridian of Segment 3 of the aft conical skirt at the circumferential coordinate, theta = 90 degrees. The following list is part of the twoskirt.OPM file corresponding to the optimized “twoskirt” design subjected to Load Case 2 (Load Set A = 10 g lateral acceleration, Load Set B = 25 psi internal ullage pressure in the propellant tank plus 200-degree uniform propellant tank cool-down plus axisymmetric non-uniform thermal loading of the aft conical skirt)

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PANDA2-type buckling predictions corresponding to the
prebuckled state along the skirt meridian at theta= 9.0000E+01 degrees...
Listed next are the assumed prebuckled state, length and
radius of the effective cylindrical shell, buckling mode,
(MSKIN,NSKIN,SLOPE), and buckling load factor for Model 1:
Buckling load factor predicted from a PANDA2-type model of
the aft skirt for Load Case 2:
Average Load Set A prebuckling resultants used in the PANDA2 model:
Average axial resultant over meridian length,NXAVE = -2.2837E+01
Average hoop resultant over meridian length,NYAVE = -1.5016E-06
Average in-plane shear resultant, NXYAVE= 2.5361E+02
Average Load Set B prebuckling resultants used in the PANDA2 model:
Average axial resultant over meridian length,NXFIX = 1.4326E+03
Average hoop resultant over meridian length,NYFIX = 6.2338E-01
Length of the equivalent cylindrical shell, FLEFF = 1.3928E+02
Radius of the equivalent cylindrical shell, RAVE = 1.3393E+02
Critical buckling mode:
Number of axial half-waves over shell length,MSKIN = 1
Number of circ. half-waves over 180 degrees, NSKIN = 23
Slope of the buckling nodal lines, SLOPE = 1.9008E-01
SLOPE=dy/dx in Fig. 9(b) of 1987 "Theoretical Basis paper.
"Bump-up" factor to adjust for milder imperfection
sensitivity factor when in-plane shear is significant 1.5000E+00
The actual buckling load factor,EIGLOC*FKNOCK/RATIO= 1.3022E+00
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The purpose of the “bump-up” factor listed here is to compensate for the use in the “tank2” formulation of a factor of safety (F.S.) for skirt buckling, TNKBUKF=2.0 (listed in Table 2) that is too high for the much milder sensitivity to initial imperfections of conical or cylindrical shells under primarily in-plane shear loading rather than uniform axial compression. In the “tank2” formulation we assume that an appropriate knockdown factor for shell buckling under primarily in-plane shear loading is $1/F.S. = 1/1.3333$ rather than $1/2.0$, which is more appropriate for axial compression of the laminated composite skirt configurations processed in this paper. The “Bump-up” factor is given by $2.0/1.3333 = 1.50$ in this particular case (Load Case 2 loading at theta=90 deg.).

Table 7 Summary of predictions from STAGS for the maximum stress components in the laminated composite parts of the skirt supports of the optimized configuration called “twoskirt”, with predictions from GENOPT/BIGBOSOR4

Aft Skirt Stresses, Load Case 1

Layer	Stress (psi)				
	Fiber Direction		Transverse Direction		Shear
	Max	Min	Max	Min	Max
1	2283	1864	-1161	-13210	2899
2	2281	1848	-1142	-13220	2900
3	17050	9339	1740	1050	2500
4	16720	9608	1740	1041	2448
5	16410	9877	1745	1031	2400
6	16140	10150	1759	1022	2357
7	15940	10410	1773	1012	2326
8	15740	10600	1787	1003	2295
9	15550	10680	1801	993	2264
10	15360	10730	1815	983	2233
11	2267	1706	-972	-13270	2907
12	2266	1691	-952	-13270	2908

Forward Skirt Stresses, Load Case 1

Layer	Stress (psi)				
	Fiber Direction		Transverse Direction		Shear
	Max	Min	Max	Min	Max
1	2912	2474	-485	-11140	2067
2	2909	2476	-473	-11150	2068
3	23790	14930	2064	1604	3580
4	23630	15140	2064	1597	3553
5	23460	15340	2063	1590	3528
6	23330	15340	2072	1584	3506
7	23190	15550	2083	1577	3485
8	23060	15730	2093	1570	3463
9	22920	15830	2104	1563	3442
10	22790	15910	2115	1557	3420
11	2890	2486	-363	-11180	2071
12	2888	2487	-351	-11180	2071

Prediction from BIGBOSOR4, Load Case 1 (only the maximum stress determined from either the aft skirt or the forward skirt appears in the GENOPT/BIGBOSOR4 output). From Table 4, Load Case 1:

Stress=2.7506E+04 psi, fiber tension: matl=2, A, seg=36, node=7, layer=10, z= 0.04

Segment 36 is the laminated composite part of Segment No. 3 of the forward skirt.

Aft Skirt Stresses, Load Case 2

Layer	Stress (psi)				
	Fiber Direction		Transverse Direction		Shear
	Max	Min	Max	Min	Max
1	3331	1361	4762	-22320	6599
2	3329	1342	4761	-22320	6598
3	31440	2460	2369	737	6422
4	31280	2840	2379	726	6399
5	31130	3220	2388	714	6381
6	31060	3594	2398	702	6373
7	31080	3970	2408	689	6368
8	31110	4099	2417	677	6365
9	31130	4132	2427	665	6361
10	31160	4153	2436	652	6357
11	3312	1164	4753	-22310	6588
12	3311	1143	4752	-22310	6586

Forward Skirt Stresses, Load Case 2

Layer	Stress (psi)				
	Fiber Direction		Transverse Direction		Shear
	Max	Min	Max	Min	Max
1	3197	1535	3668	-21290	5600
2	3195	1563	3668	-21300	5600
3	30440	3228	2320	811	6432
4	30250	3551	2324	794	6401
5	30080	3876	2334	777	6370
6	29920	4198	2344	761	6340
7	29770	4519	2354	744	6309
8	29620	4647	2364	727	6279
9	29470	4685	2373	710	6249
10	29320	4716	2383	693	6218
11	3181	1533	3663	-21340	5599
12	3180	1504	3662	-21350	5599

Prediction from BIGBOSOR4, Load Case 2 (only the maximum stress determined from either the aft skirt or the forward skirt appears in the GENOPT/BIGBOSOR4 output). From Table 4, Load Case 2:

Stress=3.4188E+04 psi, fiber tension: matl=2, A, seg=3, node=93, layer=9, z= 0.03

Segment No. 3 is in the laminated composite part of the aft skirt.